



# CF-Induction applied to Metabolic Flux Analysis

Andrei Doncescu

Katsumi Inoue

Gilles Roux

LAAS Toulouse

NII Tokyo

LAAS Toulouse

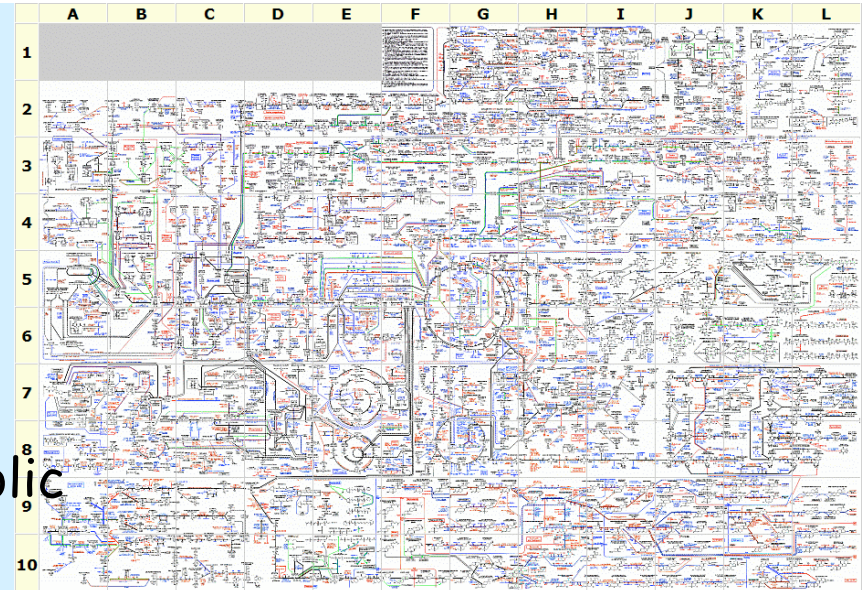
# Goal

- Explain and predict the metabolic pathway into the cell

- Generic Model :

- *Saccharomyces cerevisiae*,
- E-coli

- Inductive Logic Programming : can explain the biological knowledge



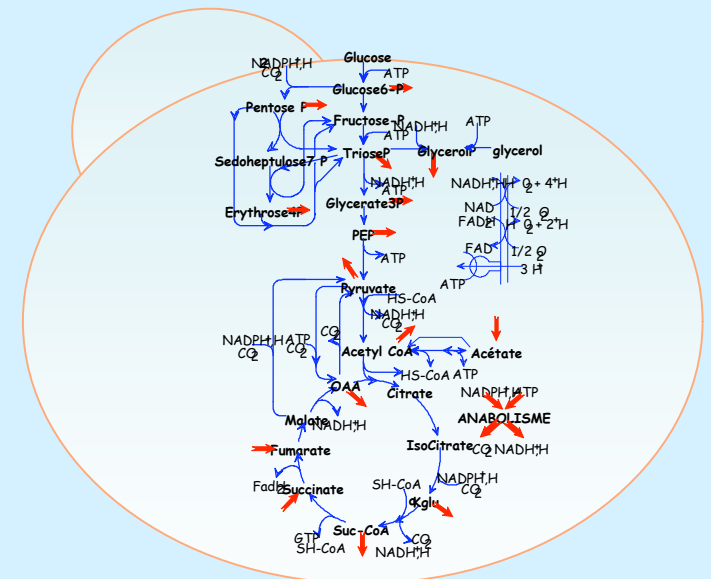
# Metabolic Flux Analysis

- Definition :

**Metabolic pathways** are sequences of enzyme-catalyzed reaction steps which convert the substrate to a variety of products to satisfy the needs of the cell.

A huge set of biochemical reactions assume the **reproduction** and the **survey** of the cell.

**Flux** is defined as the rate in which materials are processed through a metabolic pathway. The fluxes are useful to determine the maximum theoretical yields.



# Simplification of metabolic pathway

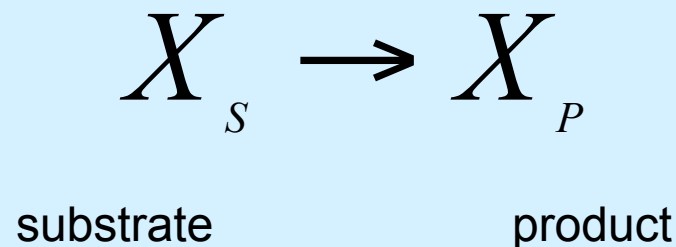
- Michaelis-Menten Reaction

$$v = v_{\max} \frac{S}{K_m + S}$$

S=substrate  
V=rate of reaction  
K=constant

Explained by a logic rule

- Mono-molecular enzymes catalized reactions :



# Metabolite Balancing

- Intracellular fluxes are determined as functions of the measurable extracellular fluxes using a stoichiometric model for major intracellular reactions and applying a mass balance around each intracellular metabolite.

$$S \cdot \underline{v} = \underline{r}$$

$S[m \times n]$  : stoichiometric matrix of metabolic network

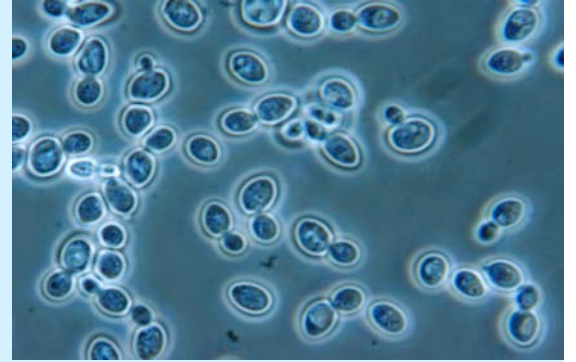
$V$  : unknown fluxes at steady state

$r$  : vector of extracellular metabolite accumulation rate

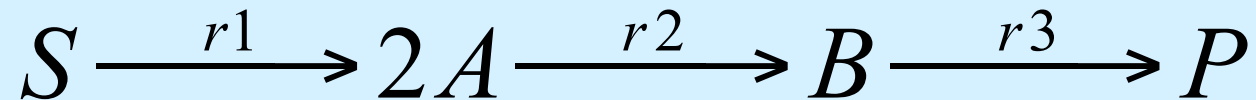
# Machine Learning Approaches

- Steady state, ignoring the temporal variance of metabolite concentration : Tamadoni-Nezdah 2004
- Integrating abduction and induction on the problem of inhibition of metabolic pathway : Muggleton et al.2006

# Modelling of Intracellular Enzyme Kinetics



- Let's take the reaction :



- The mass balance is :

$$\frac{dC_A}{dt} = 2.r_1 - r_2 \quad \frac{dC_B}{dt} = r_2 - r_3$$

Where C is the metabolite concentration  
and r is the flux

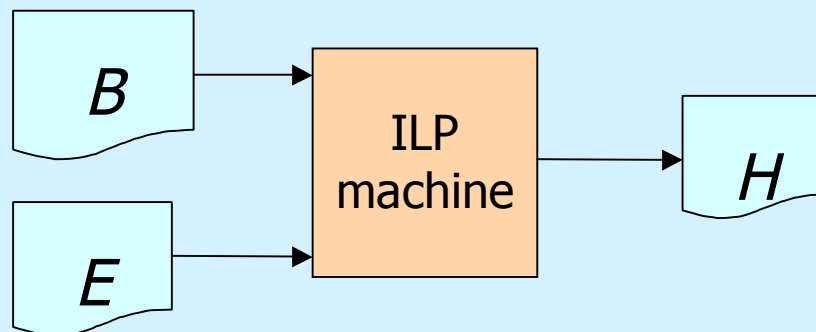
# Abduction and Induction: Logical Framework

## Input:

- $B$  : background theory
- $E$  : (positive) examples / observations

## Output:

- $H$  : hypothesis satisfying that
  - $B \wedge H \models E$
  - $B \wedge H$  is consistent.



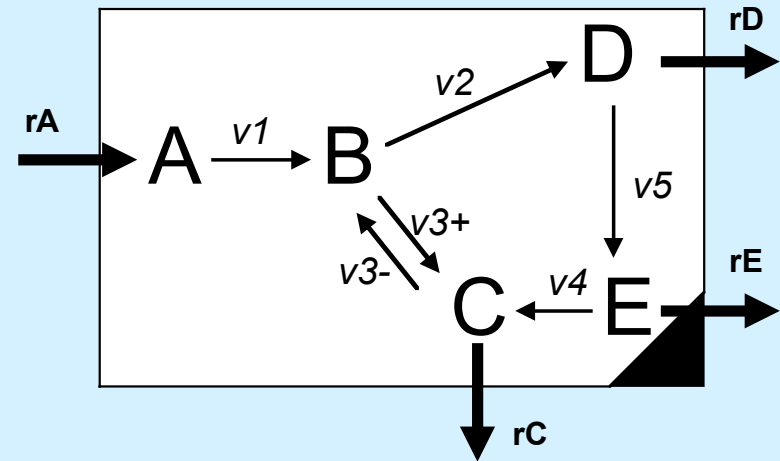


# Input of CF-induction

- `clause(e1,bg,[concentration(a,up)])`.
  - `clause(e2,obs,[concentration(d,up)])`.
  - `clause(e3,obs,[concentration(e,down)])`.
  - `clause(e4,obs,[concentration(c,down)])`.
  - `clause(e5,obs,[concentration(b,up)])`.
- The last clause is based on the fact that A and B are connected and
  - the perturbation could be propagated from A to B.

## Reaction

- `clause(bR1,bg,[reaction(a,b)])`.
- `clause(bR2,bg,[reaction(b,d)])`.
- `clause(bR3,bg,[reaction(d,e)])`.
- `clause(bR4,bg,[reaction(e,c)])`.
- `clause(bR5,bg,[reaction(c,b)])`.
- `clause(bR6,bg,[reaction(b,c)])`.



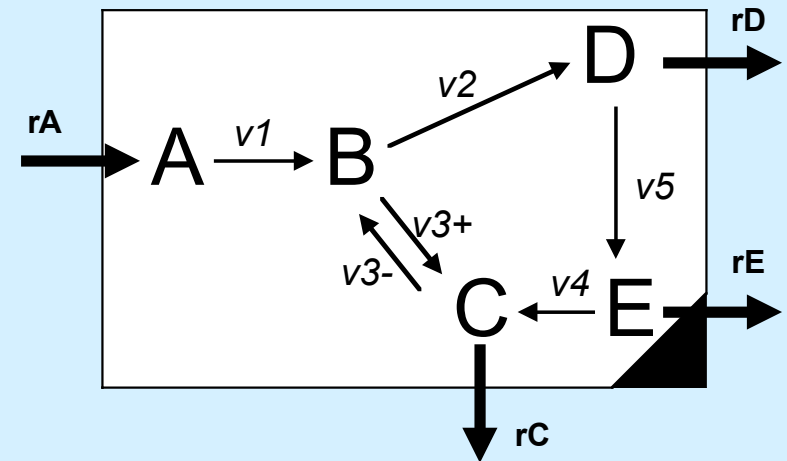
## Explanation :

`clause(be1,bg,[-reaction(Y,X),-reaction(X,Z),inhibited(Y,X),-inhibited(Y,Z),concentration(X,up)])`  
`clause(be2,bg,[-concentration(Y,down),-reaction(Y,X),inhibited(Y,X),concentration(X,down)])`

# Output of CF-induction

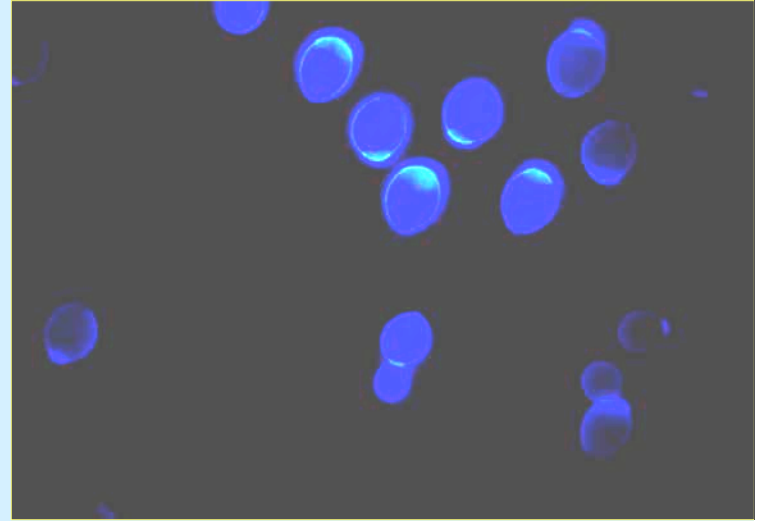
## Hypotheses:

- 1.[concentration(b, up), inhibited(b, c), inhibited(b, d), inhibited(c,b), inhibited(a, b), -concentration(a, up)]
- 2.[concentration(e, down),inhibited(c, b), inhibited(a, b),-concentration(a, up)]
- 3.[concentration(c, down), -inhibited(e, c), inhibited(c, b),inhibited(a, b),-concentration(a,up)]
- 4.[concentration(d, up), inhibited(c, b), inhibited(a, b),-concentration(a, up) ]



- The result obtained shows the possible inhibitions in the case where metabolites D,E,C are measured and an hypothesis is done about the concentration of the metabolite B.
- The interest result is obtain on the pathway B-D which explains why the metabolite concentration level in D is bigger than E, based on the non-inhibition between A-B and B-D.
- Another interesting result is the explanation of the low level concentration in C due to the inhibition on the pathway E-C.

# Conclusion



- CF-induction is able to explain metabolic pathway in a dynamic context
- The next step **diagnosis** of intracellular Enzyme Kinetics.